B.TECH THIRD SEMESTER EXAMINATION, 2008-9 COMPUTER BASED NUMERICAL & STATISTICAL TECHNIQUES PAPER CODE: TCS-302

Time: 3 Hours

M.Marks: 10

Attempt any five questions.

Q. 1.

a. Compute the real root of $x^3 - 5x + 3 = 0$ in the interval [1,2] by the Registalsi method perform three iteration only.

By Newton Raphson method find the positive root of f(u)=x - 2 sin x. choose suitable initial guess and perform three iterations.

c. Find the root of the equation $f(u)=x^3-3x-5=0$ which lies between 2 and 3 by the Muller's method. Perform two iterations only.

Q. 2

- a. Apply the quotient difference method to obtain the approximate roots of t^2 , equation. $x^3 7x^2 + 10x 2=0$
- b. Define rate of convergence. Obtain rate of convergence of Newton Raphson method.
- e. Applying Lagrange's formula, find the interpolating polynomial f(x) for the following set of observations.

| X: | 0 | 1 | 4 | 5 | _ |
|----|---|---|----|----|---|
| Y: | 4 | 3 | 24 | 39 | |

Also find f(2)

Q3.

(a) From the following table. Find the number of students who obtained less than 45 marks by method of interpolation.

| Marks: | 0-30 | 31-40 | 41-50 | 51-60 | 61-70 | 71-80 | 81 |
|----------|------|-------|-------|-------|-------|-------|----|
| No. of | 0 | 31 | 42 | 51 | 35 | 31 | 5 |
| Students | - | | | | | | |

(b) The ordinates of the normal curve are given by the following table

| X: | .0 | .2 | .4 | .6 | .8 |
|----|-------|-------|-------|-------|-------|
| Y: | .3989 | .3910 | .3683 | .3332 | .2897 |

Calculate: (i) y(.25)

(ii) y(.62)

Use Newton's method of interpolation.

(c) Use stirling's formula to find y(28) given

| X: | 20 | 25 | 30 | 35 | 40 |
|----|-------|-------|-------|-------|-------|
| Y: | 49225 | 48316 | 47236 | 45926 | 44306 |

0.4.

(a) By means of Newton's divided difference formaula, find the values of f(2). f(8) and f(15) from the following table.

| A | | | 1.0 | 111 | 12 |
|---------|-----|-----|-----|------|------|
| X: 4 | 5 | 17 | 10 | 11 | 13 |
| F(u) 48 | 100 | 294 | 900 | 1210 | 2028 |

- b . Differentiate between interpolation and curve fitting.
- c. Describe the methods of finding complex roots in detail.

Q.5.

(a) Fit a natural cubic spline to the following data:

| х . | 12 | 3 | 4 |
|-----|----|----|-----|
| V . | 11 | 49 | 121 |

Hence compute

- y(2.5) and
- y'(2) (ii)

(b) Find the first and second derivative at 1.1 for the data

| X 1.00 | 1.2 | 1.4 | 1.6 | 1.8 | 2.00 |
|--------|-------|-------|--------|-------|------|
| | | 5140 | 1 2060 | 2.432 | 4.00 |
| Y 0 | .1280 | .5440 | 1.2960 | 2.402 | |

Q.6

a. Evaluate the integral

$$\int_{X}^{2} \int_{1+x}^{3} dx$$

Sir ipson's rule taking four equal intervals and hance the value of loge 2.

Q.7. attempt any two

attempt any two

a. For a bi variate distribution
$$n = 18$$
,
$$\sum X^2 = 60, \quad \sum y^2 = 96, \quad \sum x = 12, \quad \sum y = 18, \quad \sum xy = 46$$
Find the equations of lines of regressions.

b. Fit the curve $y = ax^b$ to the following data ,using method of least

squares

| | | | | | 16 |
|--------|------|------|-----|-----|-----|
| 37 1 1 | 12 | 3 | 4 | 15 | 0 |
| XII | 12 | | 6.1 | 6.8 | 7.5 |
| V 298 | 4.26 | 5.21 | 0.1 | 0.0 | |

Write short notes on

- i.) Quality control methods
- ii.) Multiple Regression Analysis